

# **MIMO-OFDM Wireless Communications with MATLAB<sup>®</sup>**

Chapter 12. Vericide kanal bilgisini kullanmak

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# Chapter 12. Vericideki Kanal Bilgisini Kullanmak

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# Chapter 12. Vericideki Kanal Bilgisini Kullanmak

## 12.1 Vericide Kanal Kestirimi

### 12.1.1 Kanal Simetrisini Kullanmak

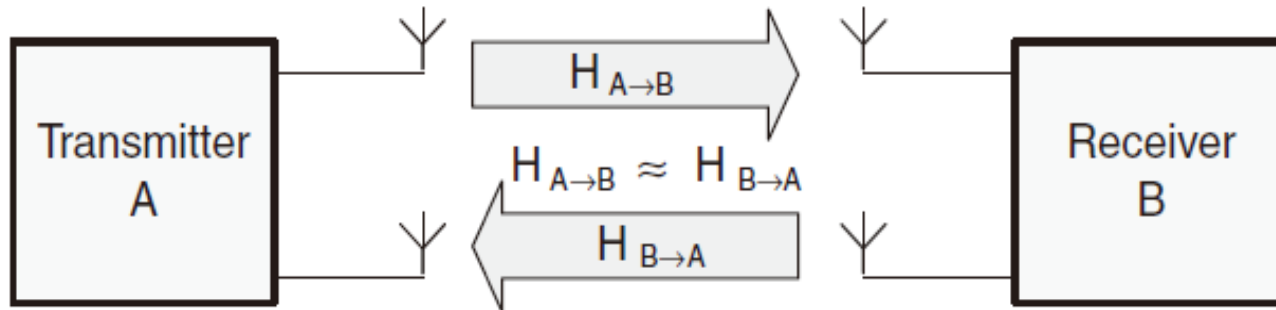
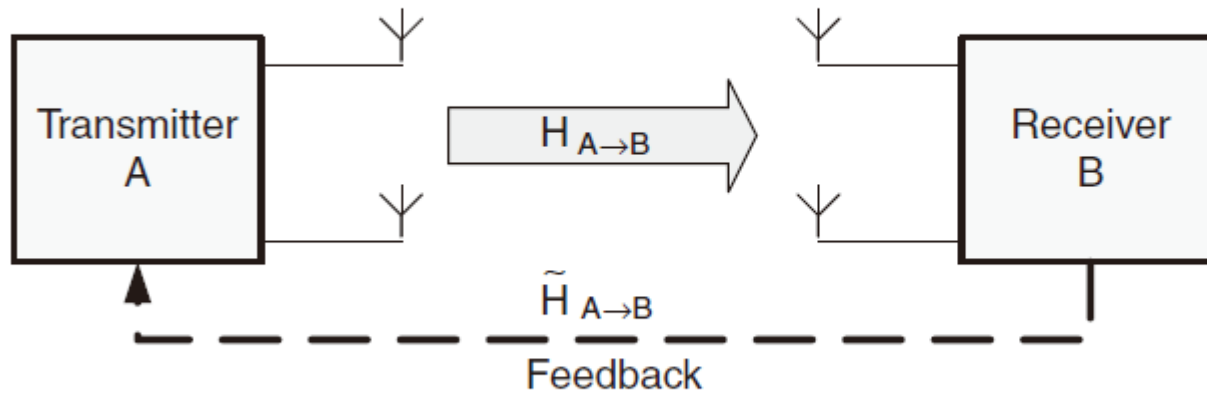


Figure 12.1 Reciprocity of wireless channel.

## 12.1.2 CSI Geribildirimi

$$\Delta_t = T_c$$

(12.1)



**Figure 12.2** Feedback of channel state information.

$$\mathbf{W}_{opt} = f(\mathbf{H}) \in \mathbf{F} = \{\mathbf{W}_1, \mathbf{W}_2, \mathbf{W}_3, \dots, \mathbf{W}_L\}$$

(12.2)

## 12.2 Ön Kodlamalı Uzay Zaman Kodu

$$\mathbf{y} = \sqrt{\frac{E_x}{N_T}} \mathbf{h} \mathbf{W} \mathbf{C} + \mathbf{z} \quad (12.3)$$

$$\Pr(\mathbf{C}_i \rightarrow \mathbf{C}_j | \mathbf{H}) = Q \left( \sqrt{\frac{\rho \|\mathbf{H} \mathbf{W} \mathbf{E}_{i,j}\|_F^2}{2N_T}} \right) \leq \exp \left( -\frac{\rho \|\mathbf{H} \mathbf{W} \mathbf{E}_{i,j}\|_F^2}{4N_T} \right) \quad (12.4)$$

$$\begin{aligned} \mathbf{W}_{opt} &= \arg \max_{\mathbf{W} \in \mathbf{F}, i \neq j} \|\mathbf{H} \mathbf{W} \mathbf{E}_{i,j}\|_F^2 \\ &= \arg \max_{\mathbf{W} \in \mathbf{F}, i \neq j} \text{Tr} \left( \mathbf{H} \mathbf{W} \mathbf{E}_{i,j} \mathbf{E}_{i,j}^H \mathbf{W}^H \mathbf{H}^H \right) \\ &= \arg \max_{\mathbf{W} \in \mathbf{F}} \text{Tr} \left( \mathbf{H} \mathbf{W} \mathbf{W}^H \mathbf{H}^H \right) \\ &= \arg \max_{\mathbf{W} \in \mathbf{F}} \|\mathbf{H} \mathbf{W}\|_F^2 \end{aligned} \quad (12.5)$$

## 12.2 Ön Kodlamalı Uzay Zaman Kodu

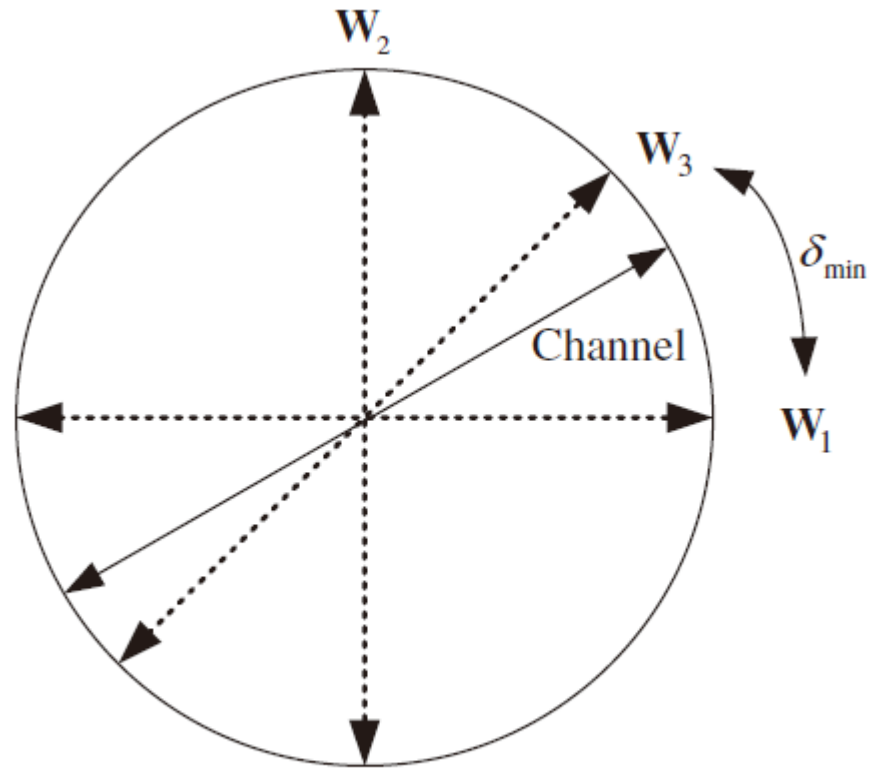
$$\mathbf{W}_{opt} = [\mathbf{v}_1 \ \mathbf{v}_2 \ \cdots \ \mathbf{v}_M] \triangleq \bar{\mathbf{V}} \quad (12.6)$$

$$E \left\{ \min_{\mathbf{W} \in \mathcal{F}} \left( \|\mathbf{H}\mathbf{W}_{opt}\|_F^2 - \|\mathbf{H}\mathbf{W}\|_F^2 \right) \right\}. \quad (12.7)$$

$$E \left\{ \min_{\mathbf{W} \in \mathcal{F}} \left( \|\mathbf{H}\mathbf{W}_{opt}\|_F^2 - \|\mathbf{H}\mathbf{W}\|_F^2 \right) \right\} \leq E \{ \lambda_1^2 \{ \mathbf{H} \} \} E \left\{ \min_{\mathbf{W} \in \mathcal{F}} \frac{1}{2} \left\| \bar{\mathbf{V}}\bar{\mathbf{V}}^H - \mathbf{W}\mathbf{W}^H \right\|_F^2 \right\} \quad (12.8)$$

$$d(\mathbf{W}_k, \mathbf{W}_l) = \frac{1}{\sqrt{2}} \left\| \mathbf{W}_k \mathbf{W}_k^H - \mathbf{W}_l \mathbf{W}_l^H \right\|_F \quad (12.9)$$

# 12.2 Ön Kodlamalı Uzay Zaman Kodu



**Figure 12.3** Precoding matrix and chordal distance.

## 12.2 Ön Kodlamalı Uzay Zaman Kodu

$$\mathbf{F} = \{\mathbf{W}_{\text{DFT}}, \boldsymbol{\theta}\mathbf{W}_{\text{DFT}}, \dots, \boldsymbol{\theta}^{L-1}\mathbf{W}_{\text{DFT}}\} \quad (12.10)$$

$$\boldsymbol{\theta} = \text{diag}\left(\left[e^{j2\pi u_1/N_T} \quad e^{j2\pi u_2/N_T} \quad \dots \quad e^{j2\pi u_{N_T}/N_T}\right]\right) \quad (12.11)$$

$$\mathbf{u} = \arg \max_{\{u_1, u_2, \dots, u_{N_T}\}} \min_{l=1, 2, \dots, N-1} d(\mathbf{W}_{\text{DFT}}, \boldsymbol{\theta}^l \mathbf{W}_{\text{DFT}}) \quad (12.12)$$



## 12.2 Ön Kodlamalı Uzay Zaman Kodu

$$\mathbf{W}_1 = \frac{1}{\sqrt{4}} \begin{bmatrix} 1 & 1 & 1 \\ 1 & e^{j2\pi \cdot 1 \cdot 2/4} & e^{j2\pi \cdot 1 \cdot 3/4} \\ 1 & e^{j2\pi \cdot 2 \cdot 2/4} & e^{j2\pi \cdot 2 \cdot 3/4} \\ 1 & e^{j2\pi \cdot 3 \cdot 2/4} & e^{j2\pi \cdot 3 \cdot 3/4} \end{bmatrix} \quad (12.13)$$

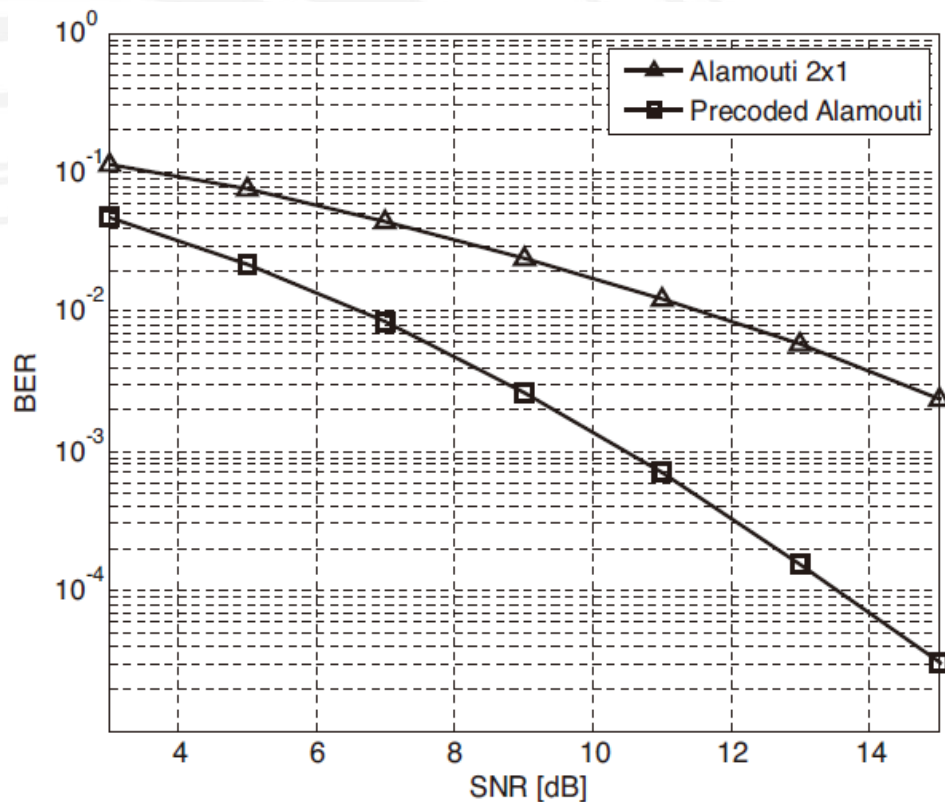
$$\mathbf{W}_i = \text{diag} \left( \left[ e^{j2\pi \cdot 1/4} \ e^{j2\pi \cdot 8/4} \ e^{j2\pi \cdot 61/4} \ e^{j2\pi \cdot 45/4} \right] \right)^{i-1} \mathbf{W}_1, \quad i = 2, 3, \dots, 64 \quad (12.14)$$

# 12.2 Ön Kodlamalı Uzay Zaman Kodu

Number of Tx antennas	Number of Data streams	Codebook size / (Feedback bits)	Column indices	Rotation vector
2	1	8/(3)	[1]	[1,0]
3	1	32/(5)	[1]	[1,26,28]
4	2	32/(5)	[1,2]	[1,26,28]
4	1	64/(6)	[1]	[1,8,61,45]
4	2	64/(6)	[0,1]	[1,7,52,56]
4	3	64/(6)	[0,2,3]	[1,8,61,45]

**Table 12.1** Codebook design parameters for OSTBC in IEEE 802.16e specification.

# 12.2 Ön Kodlamalı Uzay Zaman Kodu



**Figure 12.4** BER performance of OSTBC with and without precoding in Rayleigh fading channel.

# Kodlar

- Program 12.1 “codebook\_generator” for codebook generation
- Program 12.2 “Alamouti\_2x1\_precoding.m” for Alamouti coding with precoded OSTBC

# 12.3 Ön Kodlamalı Uzamsal Çoklrama

- Singular value decomposition

# 12.3 Ön Kodlamalı Uzamsal Çoklama

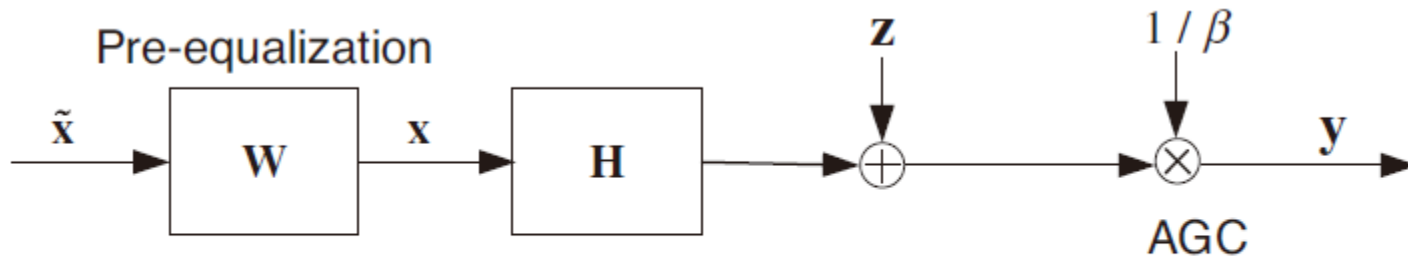


Figure 12.5 Linear pre-equalization.

$$\mathbf{x} = \mathbf{W}\tilde{\mathbf{x}} \quad (12.15)$$

$$\mathbf{W}_{ZF} = \beta\mathbf{H}^{-1} \quad (12.16)$$

## 12.3 Ön Kodlamalı Uzamsal Çoklrama

$$\beta = \sqrt{\frac{N_T}{\text{Tr}(\mathbf{H}^{-1}(\mathbf{H}^{-1})^H)}}. \quad (12.17)$$

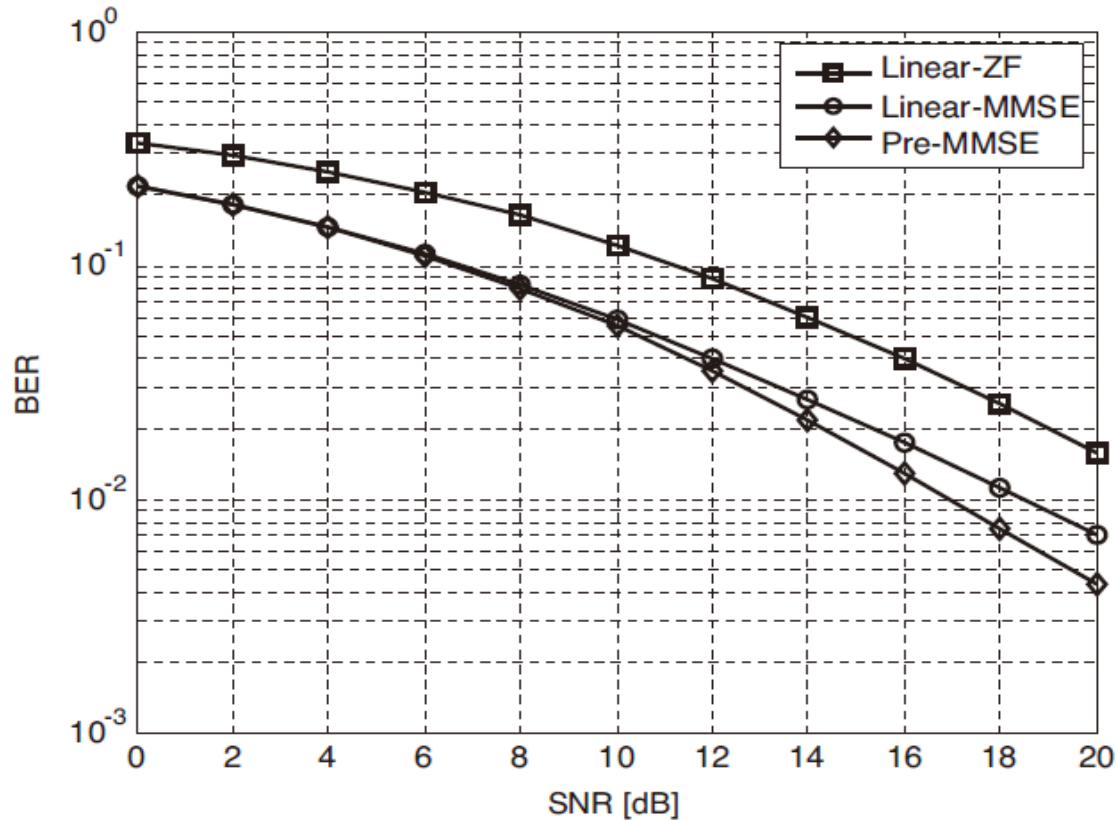
$$\begin{aligned} \mathbf{y} &= \frac{1}{\beta} (\mathbf{H}\mathbf{W}_{ZF}\tilde{\mathbf{x}} + \mathbf{z}) \\ &= \frac{1}{\beta} (\mathbf{H}\beta\mathbf{H}^{-1}\tilde{\mathbf{x}} + \mathbf{z}) \\ &= \tilde{\mathbf{x}} + \frac{1}{\beta}\mathbf{z} \\ &= \tilde{\mathbf{x}} + \tilde{\mathbf{z}}. \end{aligned} \quad (12.18)$$

## 12.3 Ön Kodlamalı Uzamsal Çoklama

$$\begin{aligned}\mathbf{W}_{MMSE} &= \beta \times \arg \min_{\mathbf{w}} E \left\{ \left\| \beta^{-1} (\mathbf{H}\mathbf{w}\tilde{\mathbf{x}} + \mathbf{z}) - \tilde{\mathbf{x}} \right\|^2 \right\} \\ &= \beta \times \mathbf{H}^H \left( \mathbf{H}\mathbf{H}^H + \frac{\sigma_z^2}{\sigma_x^2} \mathbf{I} \right)^{-1}\end{aligned}\tag{12.19}$$



# 12.3 Ön Kodlamalı Uzamsal Çoklama



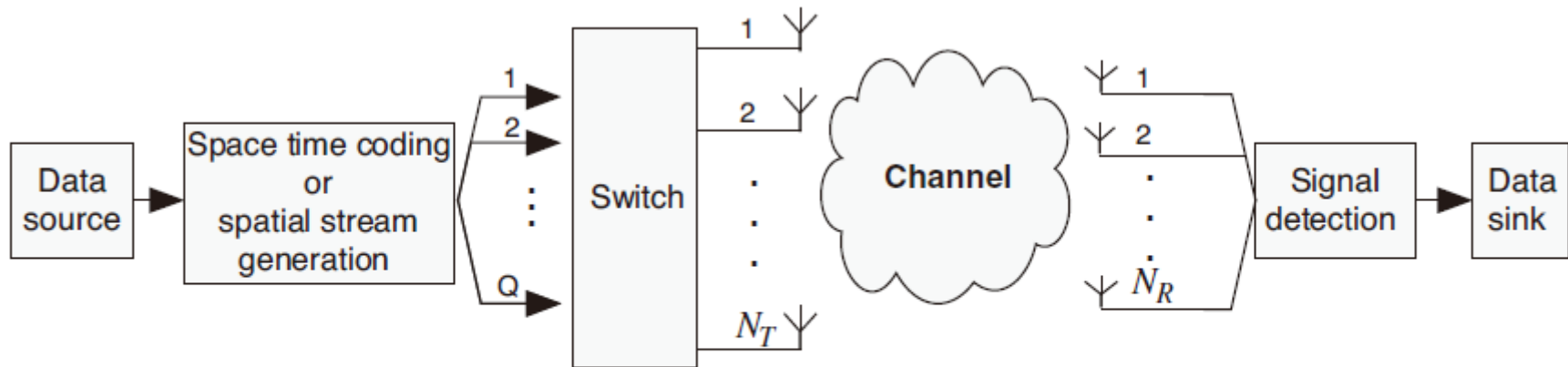
**Figure 12.6** Performance comparison: receiver-side ZF/MMSE equalization vs. pre-MMSE equalization.

# Kodlar

- Program 12.3 “pre\_MMSE.m” for Pre-MMSE equalization

# 12.4 Anten Seçim Teknikleri

$$\mathbf{y} = \sqrt{\frac{E_x}{Q}} \mathbf{H}_{\{p_1, p_2, \dots, p_Q\}} \mathbf{X} + \mathbf{z} \quad (12.20)$$



**Figure 12.7** Antenna selections with  $Q$  RF modules and  $N_T$  transmit antennas ( $Q < N_T$ ).